



# **BRICS Research Activities**

## **Algorithms**

Gerth Stølting Brodal

# Outline

- The Algorithms Group
- ALCOM  FT
- Upcoming Algorithm Events
- Algorithm Expertise within BRICS
-  CCI Europe
- Dynamic Convex Hull
- External Memory Algorithms
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# The Algorithms Group



Sven Skyum  
*Algorithms, Complexity Theory*



Erik Meineche Schmidt  
*Algorithms, Complexity Theory*



Ivan Bjerre Damgaard  
*Cryptology*



Peter Bro Miltersen  
*Complexity Theory, Data Structures*



Gudmund Skovbjerg Frandsen  
*Algebraic Algorithms, Dynamic Algorithms*



Christian Nørgaard Storm Pedersen  
*Bioinformatics, String Algorithms*



Gerth Stølting Brodal  
*Data Structures, External Memory*



Rolf Fagerberg  
*Data structures, External Memory*



Mary Cryan  
*Learning of Distributions*



Anders Yeo  
*Graph Theory, Graph Algorithms*



Peter Høyer  
*Quantum Computations*

## PhD students



Jakob Pagter  
*Time-Space Trade-Offs*



Riko Jacob  
*Optimization, Computational Geometry*



Rasmus Pagh  
*Data Structures, Hashing*



Alex Rune Berg  
*Graph Theory*

Jesper Makholm Nielsen  
*Complexity Theory*

Bjarke Skjerna  
*Algorithms*

## Algorithms and Complexity – Future Technologies

*The ALCOM-FT project is a joint effort between ten of the leading groups in algorithms research in Europe. The aim of the project is to discover **new algorithmic concepts**, identify **key algorithmic problems** in important applications, and contribute to the accelerated **transfer of advanced algorithmic techniques** into commercial systems.*

*The project takes place from June 2000 to June 2003. It is supported by the European Commission under the Information Society Technologies programme of the Fifth Framework, as project number IST-1999-14186.*

- ALCOM-FT is a continuation of ALCOM, ALCOM-II, ALCOM-IT
- BRICS is the coordinator of ALCOM-FT

# ALCOM-FT Sites

BRICS

Erik Meineche Schmidt

Barcelona

Josep Díaz

Cologne

Michael Jünger

INRIA Rocquencourt

Philippe Flajolet

Max-Planck-Institut für Informatik

Kurt Mehlhorn

Paderborn

Burkhard Monien

Friedhelm Meyer auf der Heide

Patras

Paul Spirakis

Rome “La Sapienza”

Giorgio Ausiello

Utrecht

Jan van Leeuwen

Warwick

Mike Paterson

# Upcoming Algorithm Events

## August 28–31, 2001

ESA 2001 – 9th Annual European Symposium on Algorithms

WAE 2001 – 5th Workshop on Algorithm Engineering

## Summer 2002

Summer school on “External Memory Algorithms”

## Ongoing

Alcom seminar

# Algorithm Expertise within BRICS

- Algorithms in general
- Data structures
- Dynamic algorithms
- External memory algorithms
- Algorithm engineering / experimental algorithmics

- Domain specific project
- “Automatic layout of JyllandsPosten’s JobSection”
- Problem  $\approx$  2D bin packing
- 2-approximation ?
- Enumeration + heuristics
- BRICS people
  - Kristian Høgsberg
  - Riko Jacob
  - Anders Yeo
  - Gerth Stølting Brodal
  - Erik Meineche Schmidt

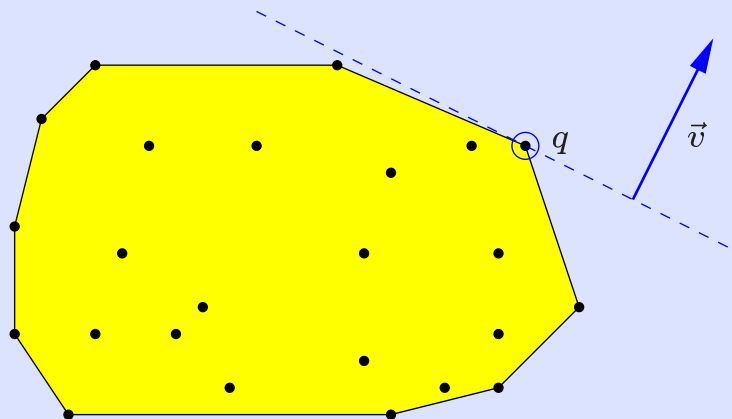




# Dynamic Convex Hull

Insert( $p$ ), Delete( $p$ )    Insert/delete a point  $p$

Query( $\vec{v}$ )    Find extreme point on CH in direction  $\vec{v}$



Overmars  
van Leeuwen 1981

Chan 1999

Brodal  
Jacob 2000

Updates	$O(\log^2 n)$	$O(\log^{1+\varepsilon} n)$	$O(\log n \cdot \log \log n)$
Queries	$O(\log n)$	$O(\log n)$	$O(\log n)$

# External Memory Algorithms

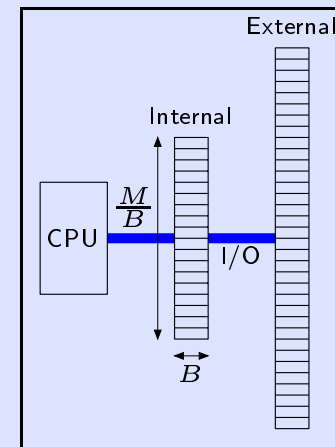
I/O model [Aggarwal and Vitter]

$M$  = Internal memory size

$N$  = Problem size

$B$  = Block size

Complexity = # block I/Os to solve a problem



## Examples

$$\text{Scan}(N) = O\left(\frac{N}{B}\right)$$

$$\text{Sort}(N) = O\left(\frac{N}{B} \cdot \log_{M/B} \frac{N}{M}\right)$$

## Minimum Spanning Tree (MST)

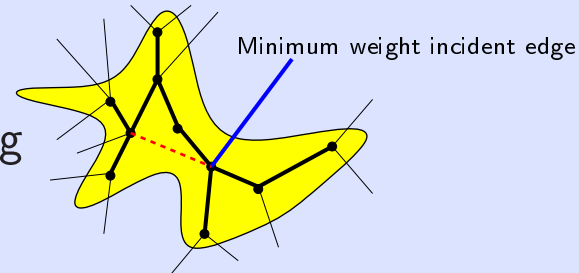
Compute the MST of a weighted graph with  $V$  vertices and  $E$  edges

Internal	External
Chazelle 1999	Arge, Brodal, Toma 2000
$O(E \cdot \alpha(E, V))$	$O(\text{Sort}(E) \cdot \log \log \frac{V \cdot B}{E})$

# Minimum Spanning Tree

## Prim's algorithm

Grow a single tree by iteratively including a minimum weight incident edge



Priority queue on incident edges

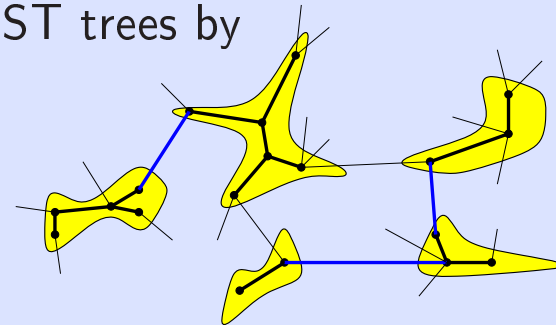
- Internal  $O(E \cdot \log E)$
- External  $O(\underbrace{V}_B + \text{Sort}(E))$   
bottleneck if  $V \cdot B = \Omega(E)$

## Kruskal's algorithm

In  $O(\log V)$  phases grow independent MST trees by picking minimum weight incident edges

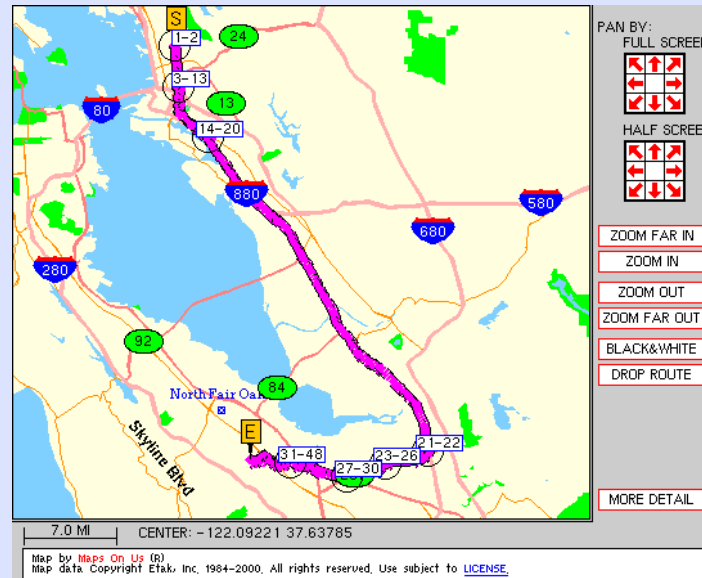
Internal  $O(E \cdot \log V)$

External  $O(\text{Sort}(E) \cdot \log V)$



Using "superphases"  $V \rightarrow \frac{V}{k}$  requires  $O(\text{Sort}(E) \cdot \log \log k)$  I/Os

Let  $k = \frac{V \cdot B}{E}$  and switch to Prim implies the external result □



*“However, because of the size of the routing data, we have to use **heuristics** when planning routes (i.e., we find “close to optimum” routes rather than optimum routes). As a result, sometimes a Favor Highways route will be slightly faster than the Fastest route. This is particularly true for routes longer than about 100 miles. ... Our routing will continually improve as the quality of our data improves and as we **invent better routing algorithms**.”*